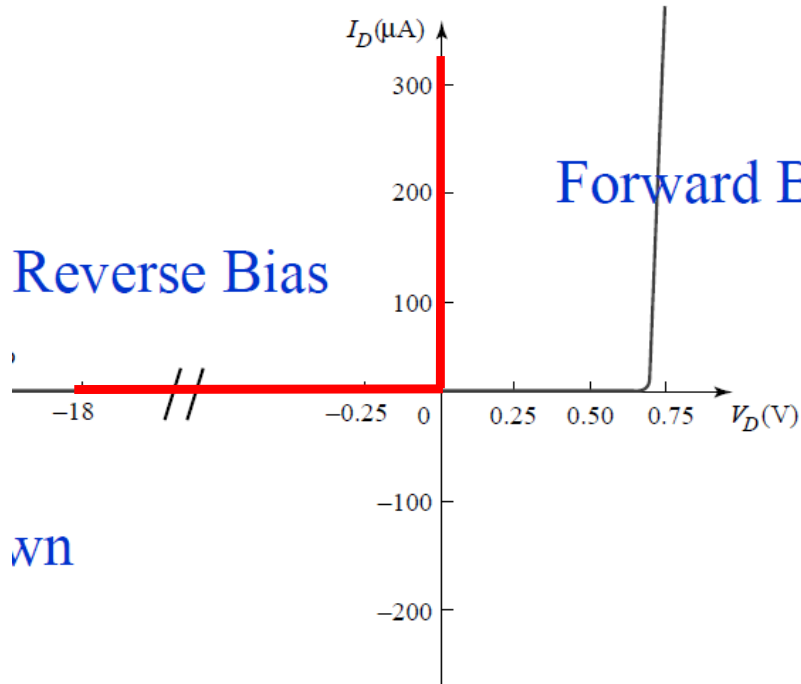


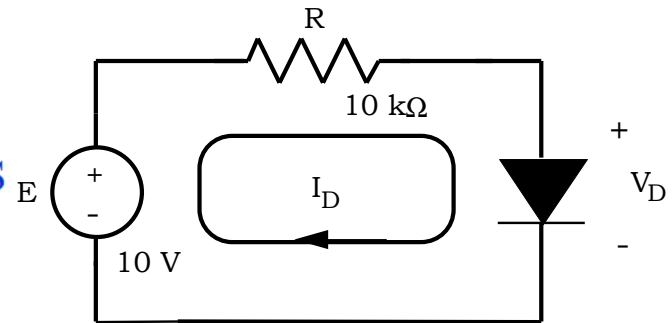
DIODE CIRCUITS

- 1 DC and low-frequency diode models**
- 2 The diode-resistance circuit**
- 3 Peak and power detectors**
- 4 Rectifiers**
- 5 Thermal sensor**

Ideal diode model



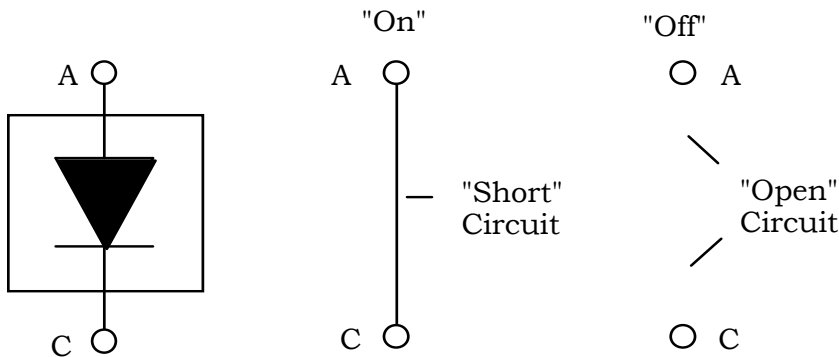
vn



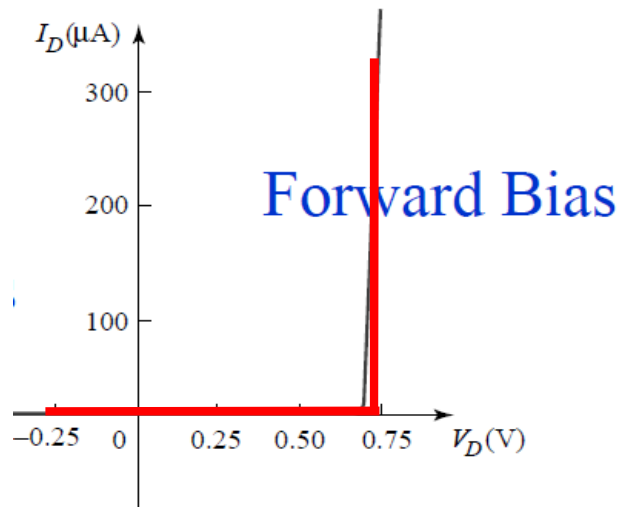
$$I_D = \frac{E - V_D}{R}$$

$$I_D = \frac{10V}{10k \Omega}$$

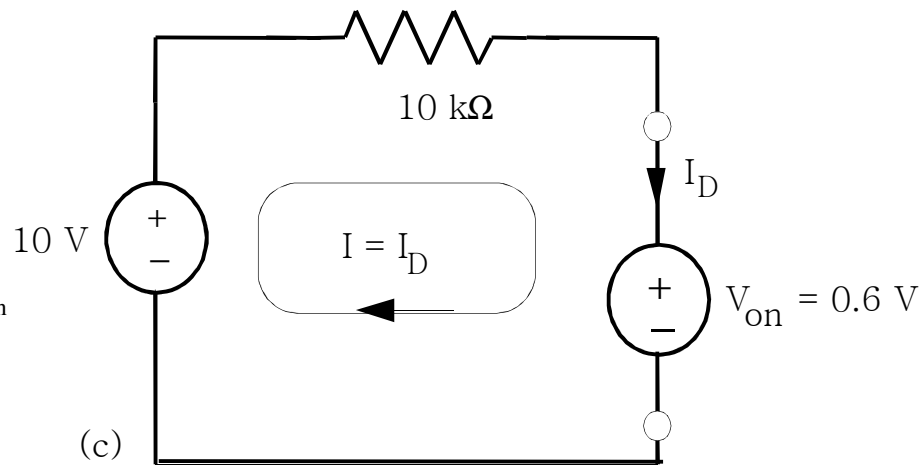
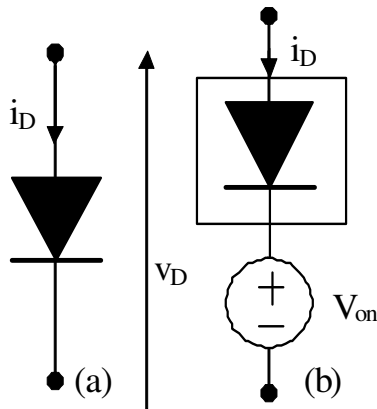
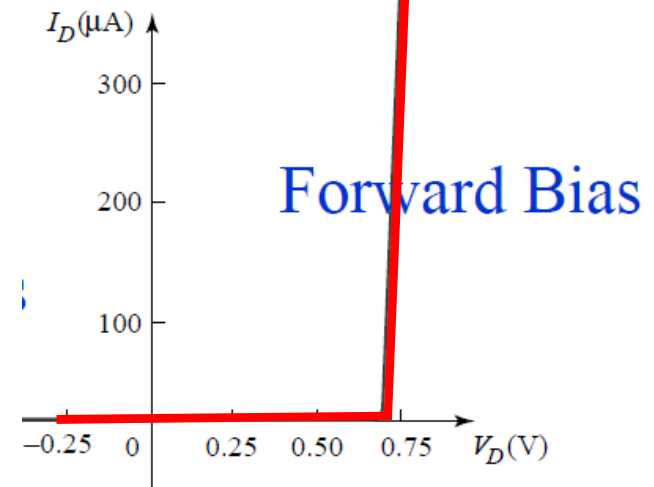
$$I_D = 1mA$$



- **Constant-voltage-drop model**



- **Constant-voltage-drop + resistance model**

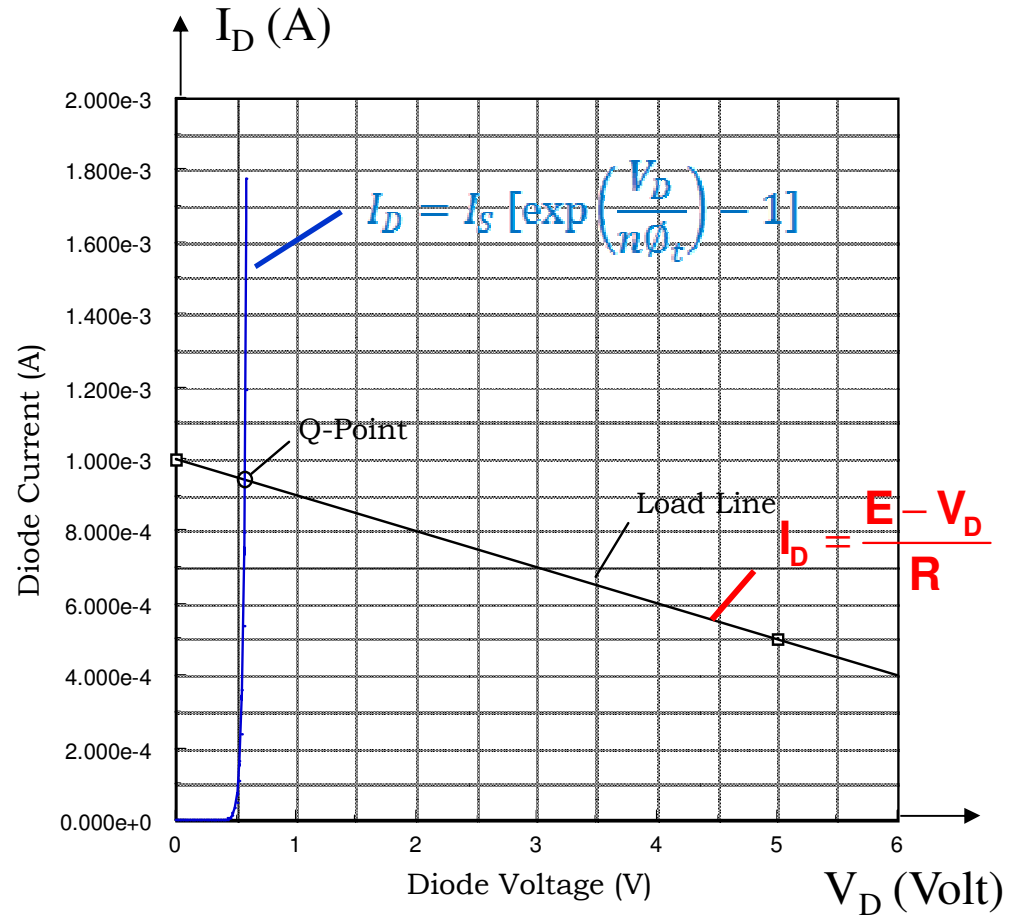
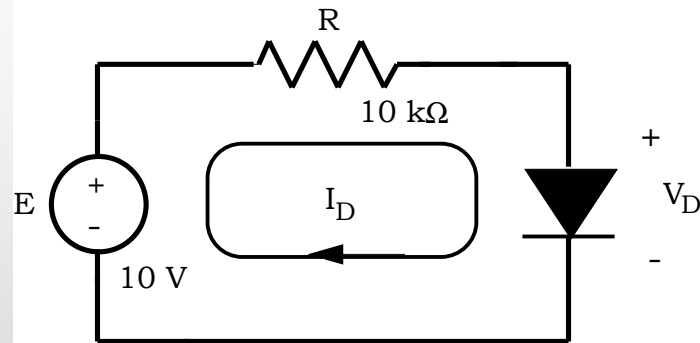


$$I = \frac{10 - 0.6}{10 \text{ k}\Omega}$$

$$I = 0.94 \text{ mA}$$

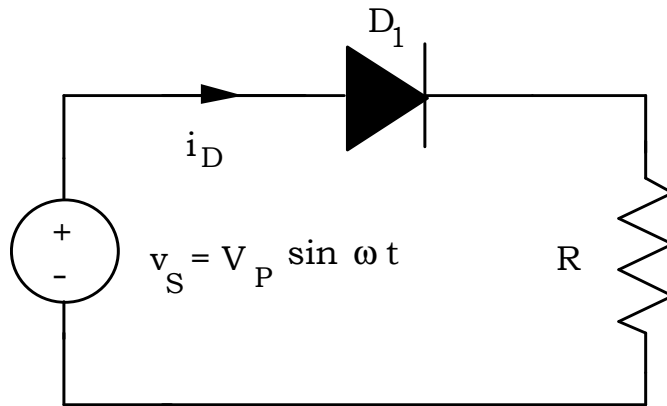
What if the input voltage is 1 V? 0.1V?

Graphical analysis



Diode i-v characteristic and load line

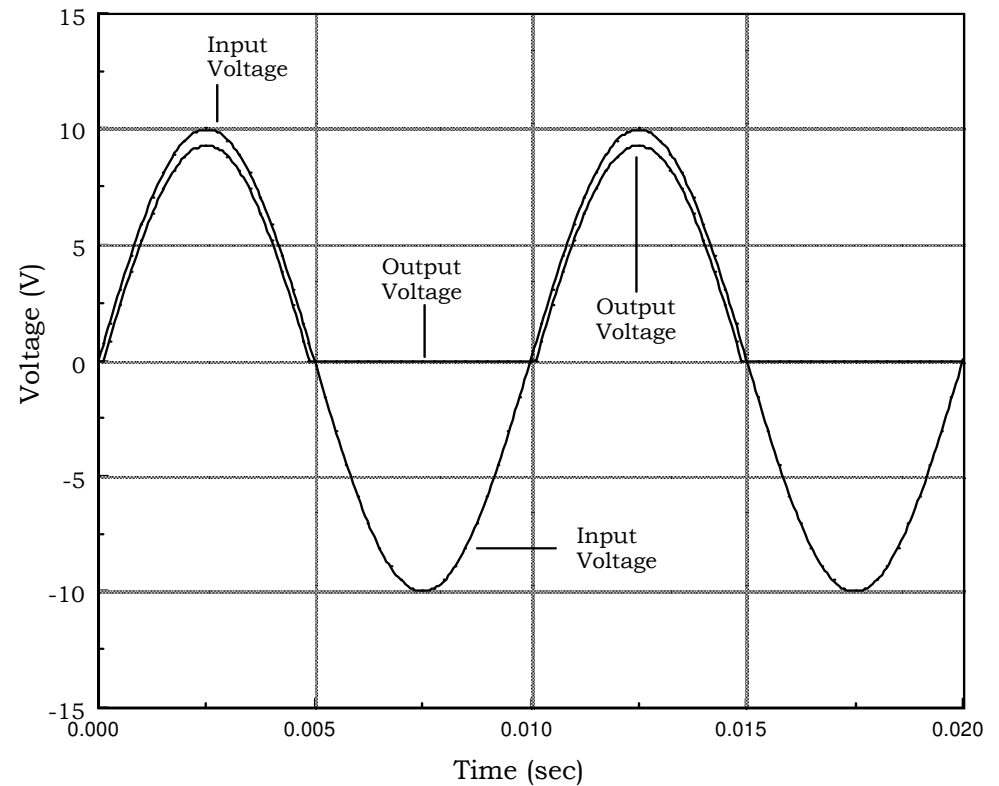
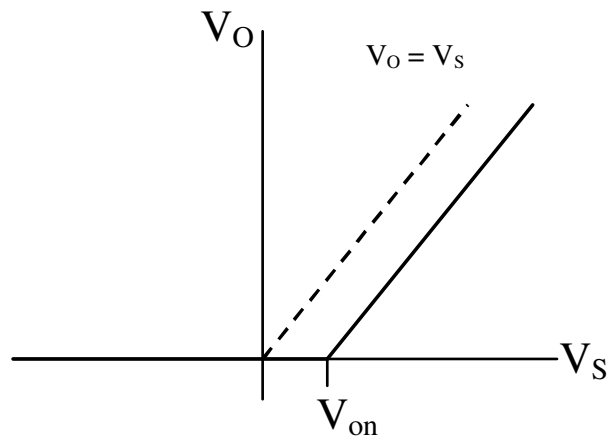
Half-wave rectifier circuit: resistive load



Simplified analysis

$V_S \leq V_{on} \rightarrow$ Diode is ON

$V_S > V_{on} \rightarrow$ Diode is OFF

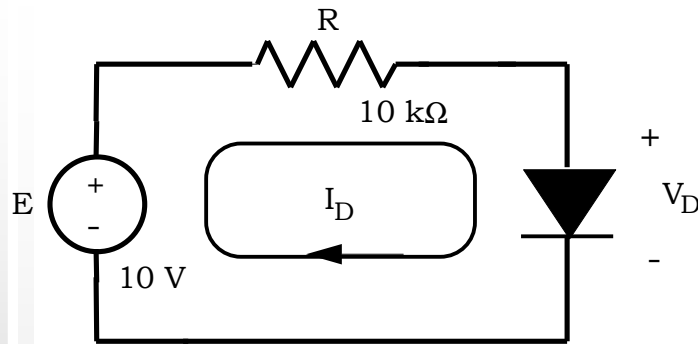


$V_p = 10 \text{ V}$ and $V_{on} = 0.7 \text{ V}$

If $V_p \gg V_{on}$

$$\bar{i}_D = \frac{1}{\pi} \frac{V_p}{R} \quad (\text{average value})$$

$$i_{Dmax} = \frac{V_p}{R} \quad PIV = V_p$$



If you know I, it is simple to calculate E

$$E = RI + n\phi_t \ln\left(\frac{I}{I_s} + 1\right)$$

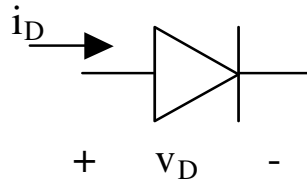
Example:

R= 10 kΩ,

I_S=1 nA, nφ_t = 50 mV

As you can see, for this specific example the resistor does not play an important role for current less than 1 μA whereas the diode voltage drop is small for currents greater than, say, 1 mA.

I/I _S	E (mV)
0	0
1	50 ln2
9	50 ln10
10 ³	10+50 ln10 ³
10 ⁶	10 ⁴ + 50 ln10 ⁶
-0.5	-50 ln2
-0.9	-50 ln10
-1	-∞
-9	???????

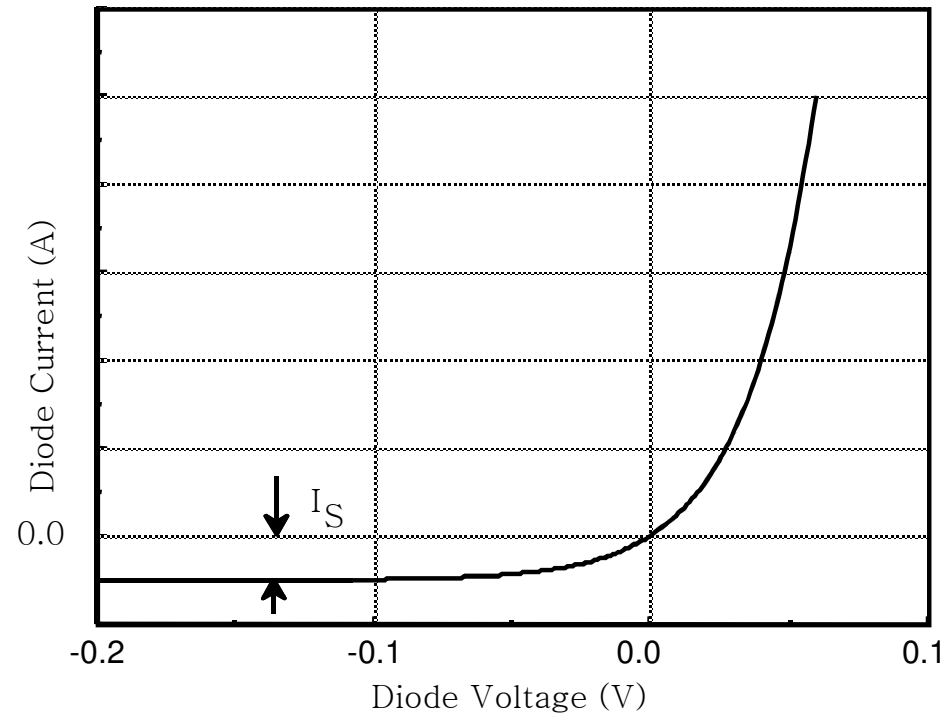


$$\phi_t = kT/q$$

$$i_D = I_S \left[\exp\left(\frac{V_D}{n\phi_t}\right) - 1 \right]$$

$$\phi_t \cong 25 \text{ mV @ } 290 \text{ K}$$

$$n \sim 1 \text{ to } 1.5$$



In an IC implementation, most diodes (or diode-connected MOSFETs)

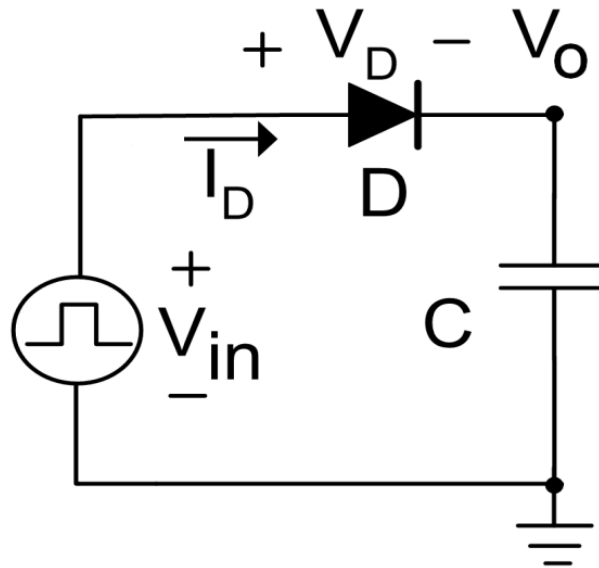
can be represented by Shockley equation.

I_S (saturation current)- design parameter.

Voltage rectifier: fundamentals

A simple case: square-wave input

Steady-state analysis



Basic principle: charge conservation/
average current through diode = 0

$$\frac{1}{T} \int_{-T/2}^{T/2} I_D dt = 0 \quad I_D = I_S \left[e^{\frac{V_D}{n\phi_t}} - 1 \right]$$

$$\frac{I_S}{T} \left[\int_{-T/2}^0 \left(e^{\left(\frac{-V_P - V_o}{n\phi_t} \right)} - 1 \right) dt + \int_0^{T/2} \left(e^{\left(\frac{V_P - V_o}{n\phi_t} \right)} - 1 \right) dt \right] = 0$$

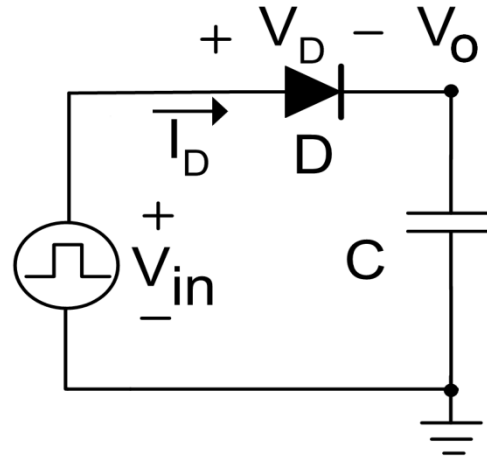
Assumption: very low ripple (high C)

→ $V_o \cong \text{constant}$

$$\frac{V_o}{n\phi_t} = \ln \left[\frac{e^{V_P/n\phi_t} + e^{-V_P/n\phi_t}}{2} \right] = \ln \left[\cosh(V_P/n\phi_t) \right]$$

Power/Peak Detector

A simple case: square-wave input



$$\frac{V_o}{n\phi_t} = \ln \left[\cosh \left(\frac{V_P}{n\phi_t} \right) \right]$$

Power Detector

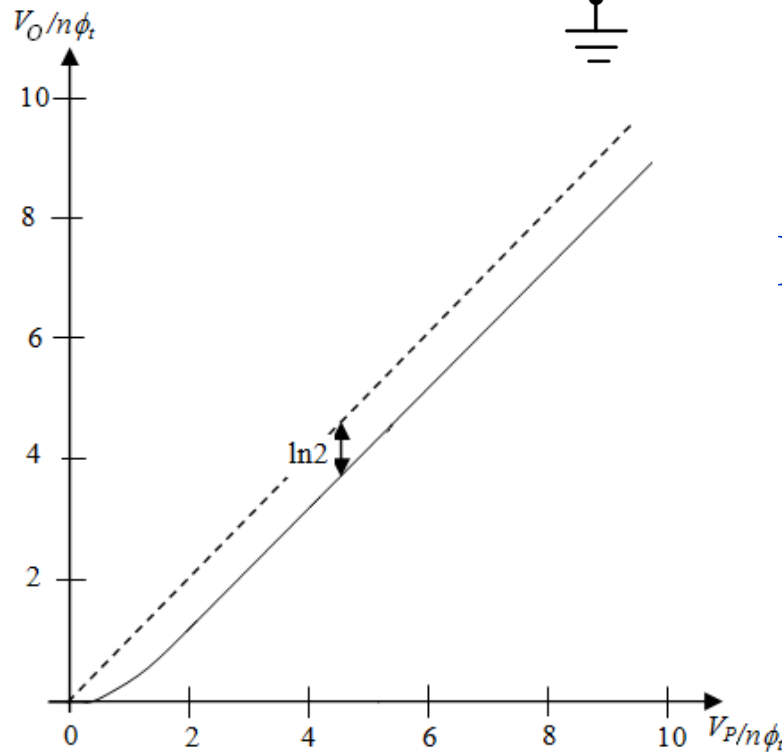
$$V_P \ll n\phi_t \rightarrow \frac{V_o}{n\phi_t} \cong \frac{1}{2} \left(\frac{V_P}{n\phi_t} \right)^2$$

Peak Detector

Diode "ON"
voltage drop

$$V_P \gg n\phi_t \rightarrow V_L \cong V_P - \underbrace{n\phi_t \ln 2}_{\text{Why?}}$$

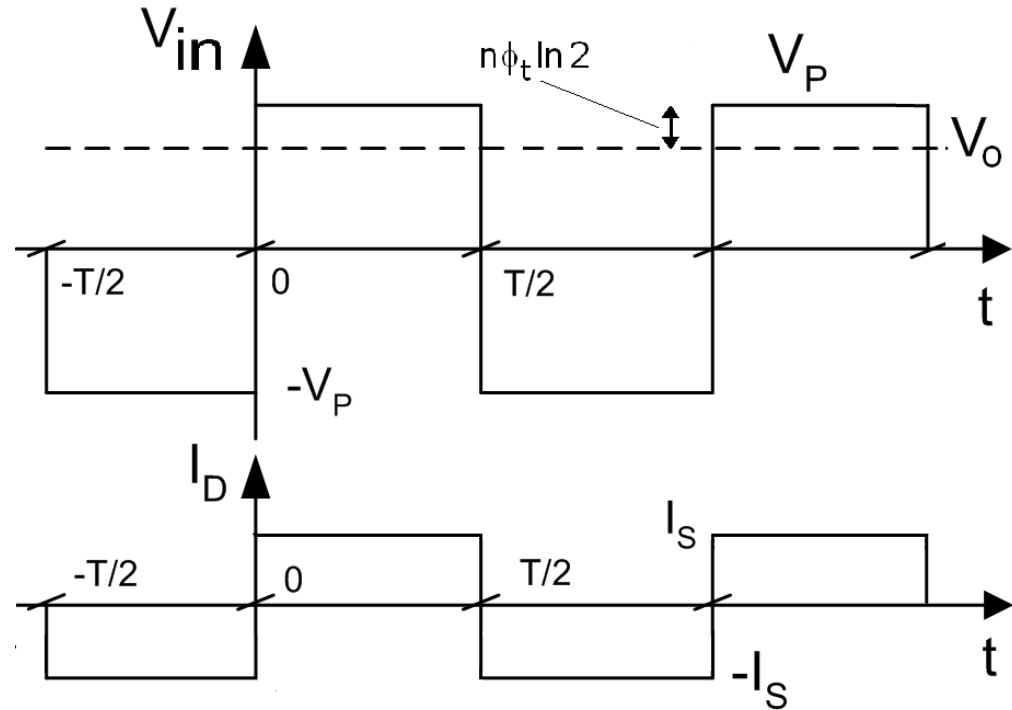
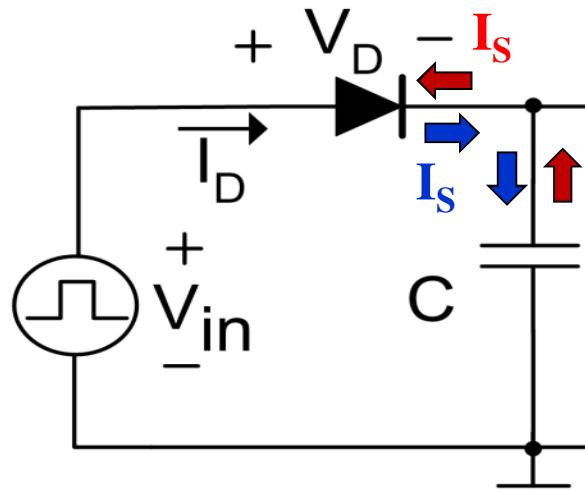
Input ↖ ↖



Results for sine input are similar.
Difference is a "form factor"

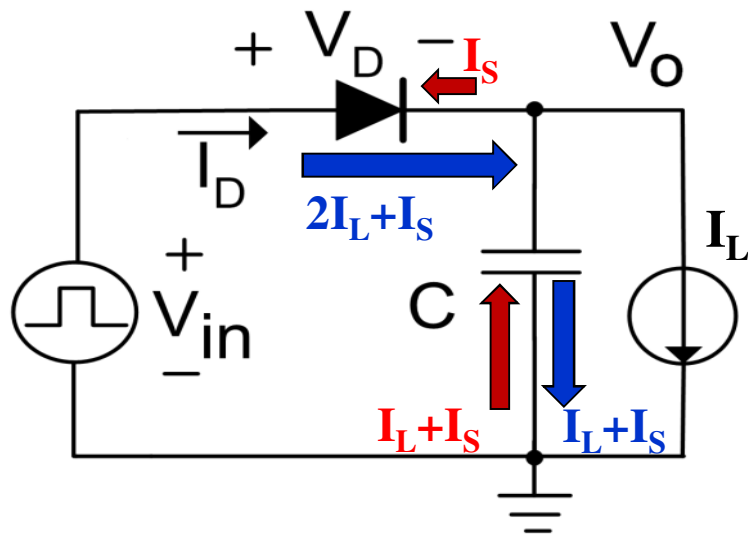
Voltage rectifier: fundamentals

A simple case: square-wave input



Waveforms for $V_P \gg n\phi_t$

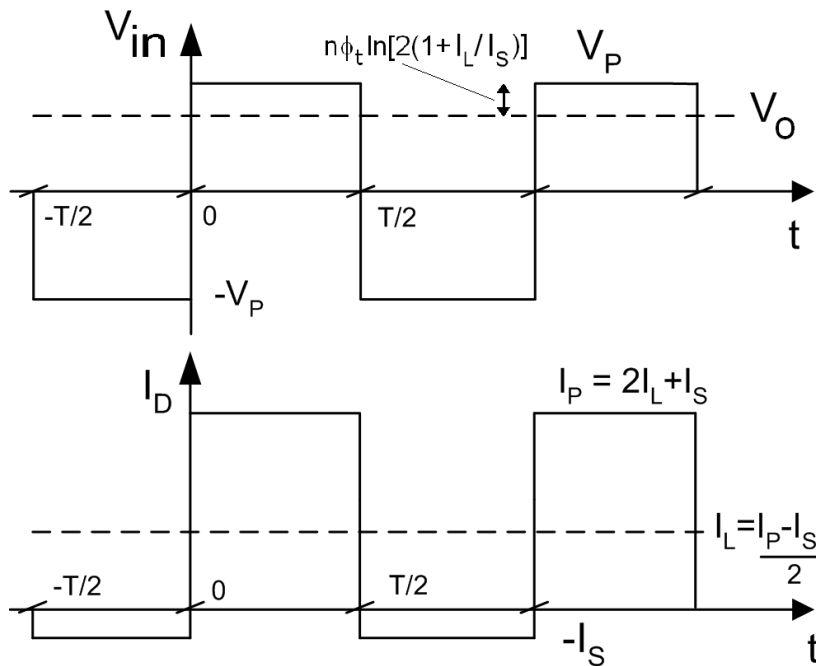
Voltage rectifier: fundamentals



Steady-state analysis

$$\frac{I_S}{T} \left[\int_{-T/2}^0 \left(e^{\left(\frac{-V_P - V_o}{n\phi_t} \right)} - 1 \right) dt + \int_0^{T/2} \left(e^{\left(\frac{V_P - V_o}{n\phi_t} \right)} - 1 \right) dt \right] = I_L$$

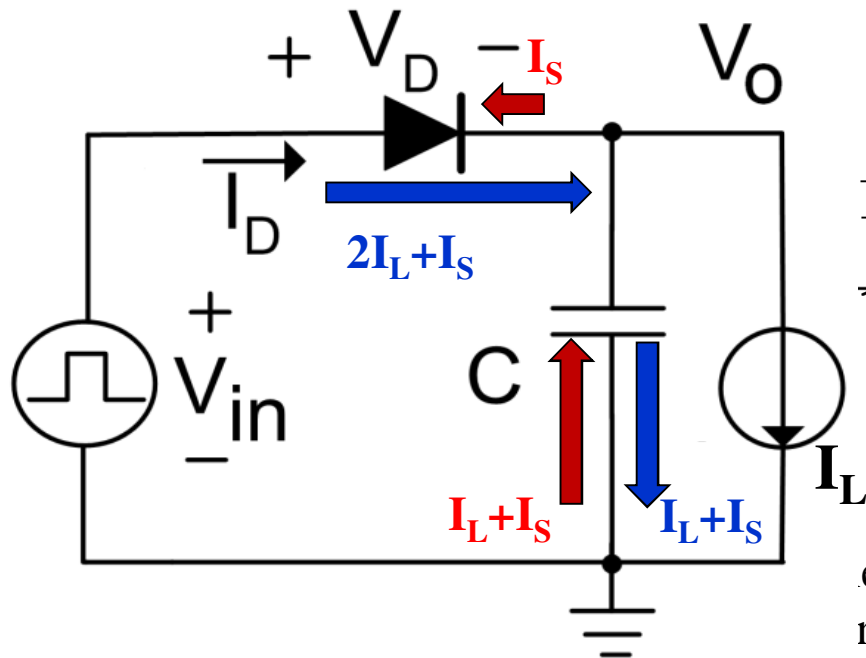
Assumption: very low ripple $\rightarrow V_o \cong \text{constant}$



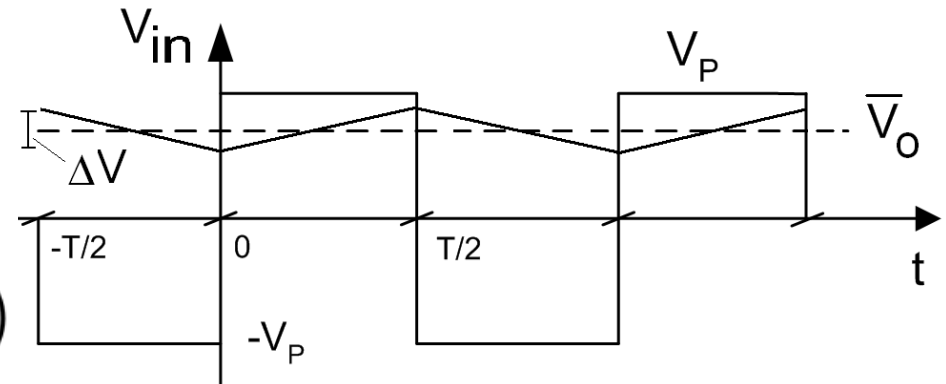
$$\frac{V_o}{n\phi_t} = \ln \left[\frac{\cosh(V_P / n\phi_t)}{1 + I_L / I_S} \right]$$

Waveforms for $V_P \gg n\phi_t$

Voltage rectifier: fundamentals



Output voltage ripple



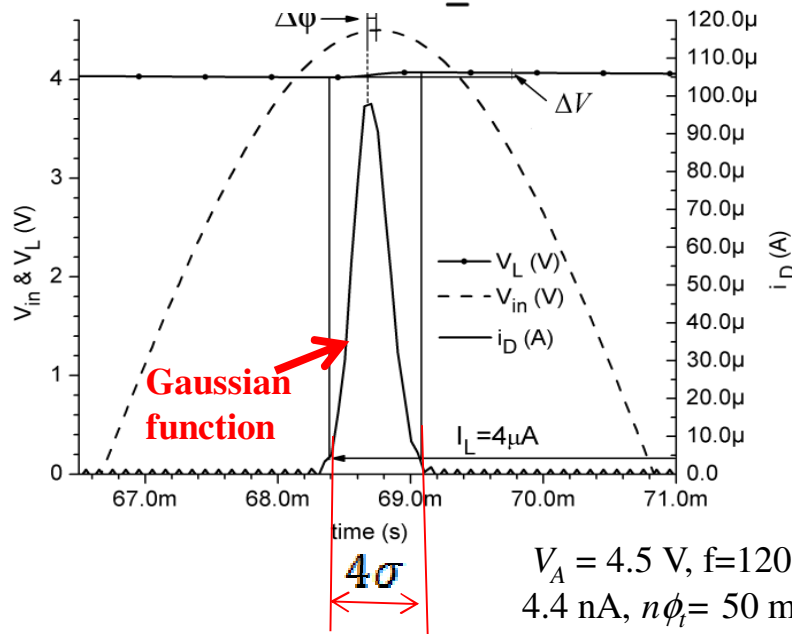
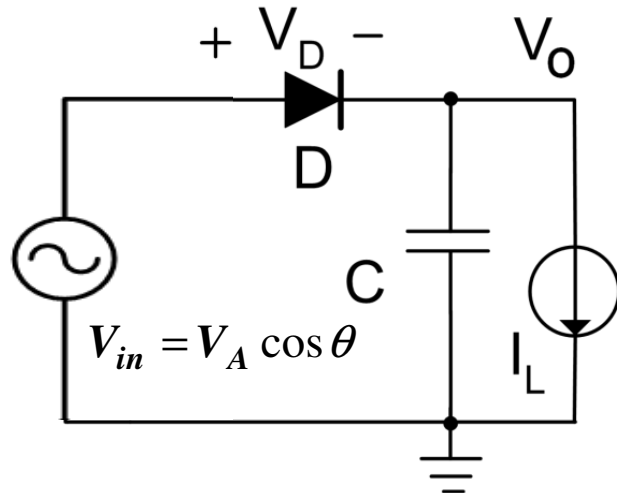
The discharge rate of the capacitor during the negative half-cycle of the input is

$$I_C = \frac{dQ_C}{dt} = C \frac{dV_C}{dt} \cong I_L + I_S$$

$$\int_{-T/2}^0 dV_C = \Delta V \cong \frac{I_L + I_S}{C} \frac{T}{2} = \frac{I_L + I_S}{2fC}$$

Voltage rectifier: fundamentals

Sine-wave input



$V_A = 4.5 \text{ V}$, $f = 120 \text{ Hz}$, $I_L = 4 \mu\text{A}$. $I_S = 4.4 \text{ nA}$, $n\phi_t = 50 \text{ mV}$, $C = 150 \text{ nF}$.

Steady-state analysis

Basic principle: charge conservation

$$\frac{1}{T} \int_{-T/2}^{T/2} I_D dt = I_L \quad I_D = I_S \left[e^{\frac{V_D}{n\phi_t}} - 1 \right]$$

$$\frac{I_S}{2\pi} \left[\int_{-\pi}^0 \left(e^{\left(\frac{-V_A \cos\theta - V_o}{n\phi_t} \right)} - 1 \right) d\theta + \int_0^{\pi} \left(e^{\left(\frac{V_A \cos\theta - V_o}{n\phi_t} \right)} - 1 \right) d\theta \right] = I_L$$

Assumption: very low ripple (high C)

$\rightarrow V_o \cong \text{constant}$

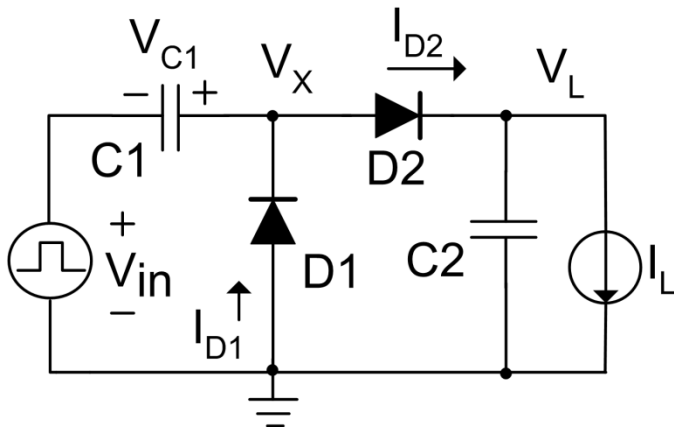
$$\frac{V_o}{n\phi_t} = \ln \left[\frac{I_0 (V_A / n\phi_t)}{1 + I_L / I_S} \right]$$

$$I_0(z) = \frac{1}{\pi} \int_0^{\pi} e^{z \cos\theta} d\theta$$

modified Bessel function of the first kind of zero order

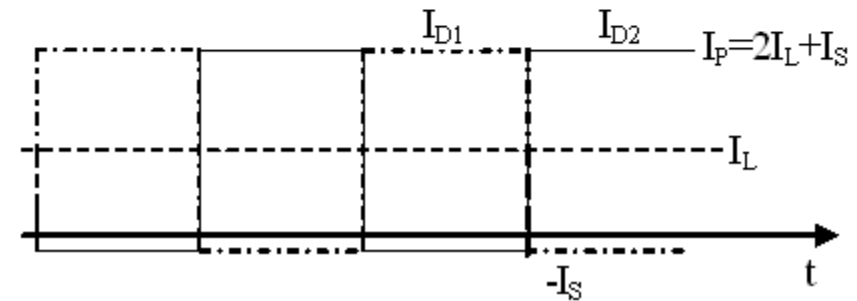
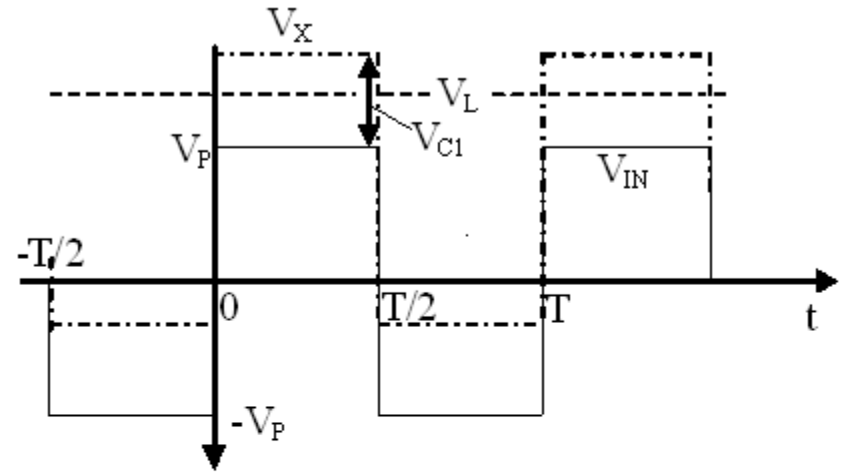
The voltage multiplier

Voltage doubler → Clamping circuit & peak detector



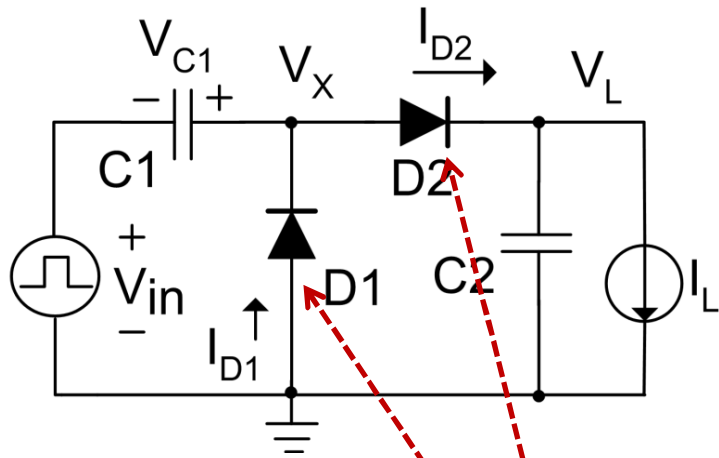
$D1$, $C1$, and V_{in} → half-wave rectifier.
 V_{C1} stored in $C1$ is a dc voltage equal to that of a half-wave rectifier. $V_X = V_{in} + V_{C1}$. The dc output voltage of the doubler is equal to the value calculated for the half-wave rectifier plus V_{C1} .

$$V_L = 2V_{C1}$$



The voltage multiplier

Voltage doubler



$$PCE = \frac{P_{load}}{P_{in}} = \frac{V_L I_L}{P_{load} + P_{loss}}$$

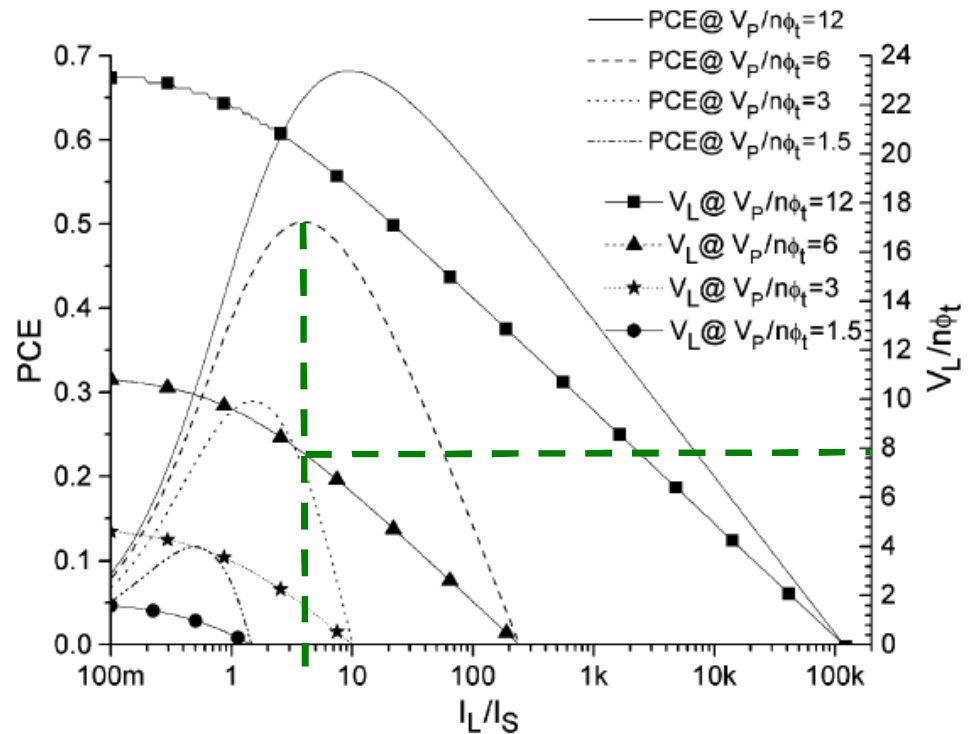


Fig. 3. Power conversion efficiency and load voltage of the voltage doubler versus normalized load current for values of $V_P/n\Phi_t$ equal to 1.5, 3, 6, and 12.

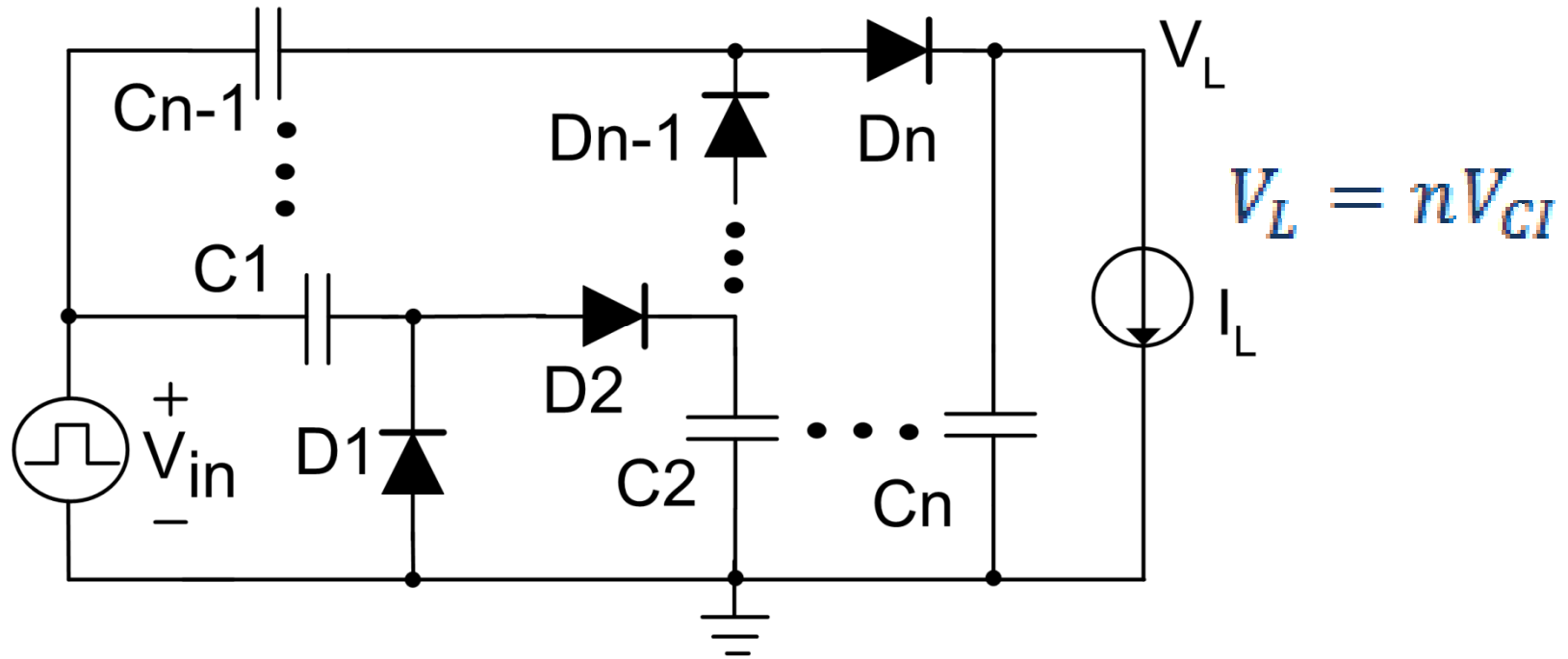
$$PCE_{max} = PCE @ \frac{V_L}{2(N)n\Phi_t} = \frac{I_L}{I_S}$$

PCE: Power Conversion Efficiency

Voltage doubler

N-stage voltage multiplier

The voltage multiplier

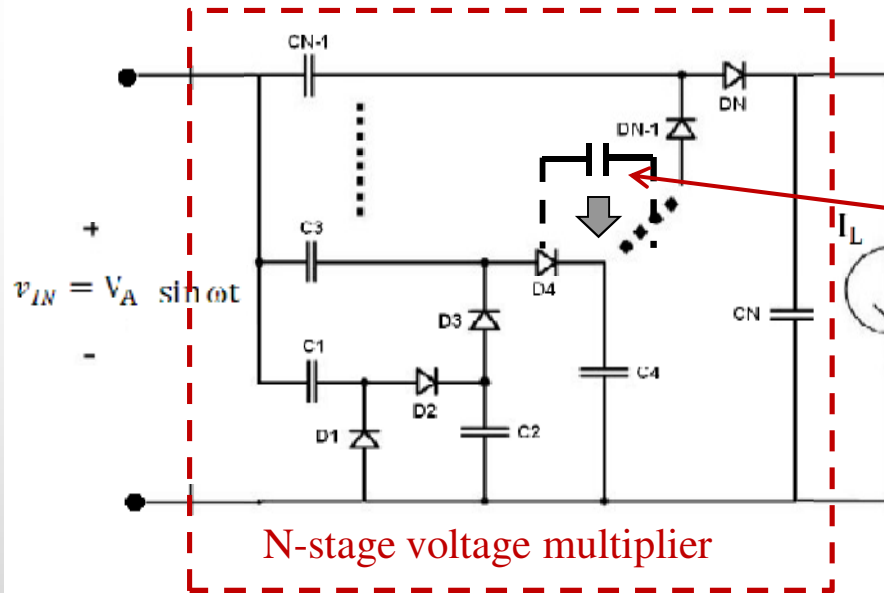


N-stage voltage multiplier

Applications:

- Generation of voltages higher than the supply voltage, for EEPROMs, flash memories
- Energy harvesting for RFID tag chips, for example

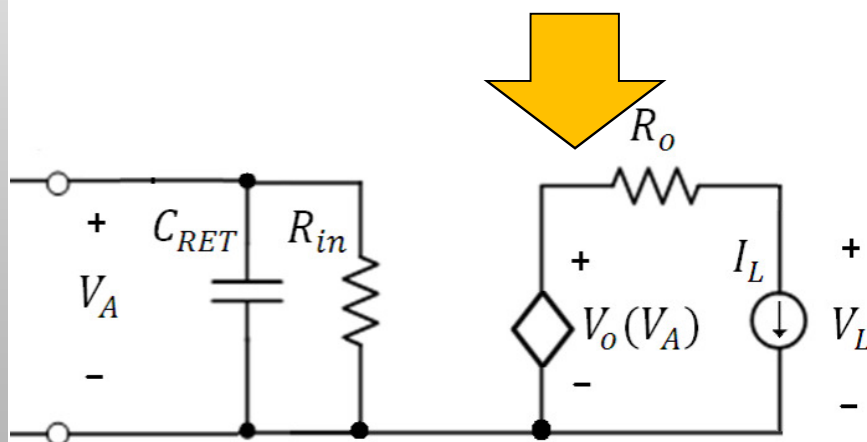
The voltage multiplier model



Average diode capacitance

$$\frac{V_L}{Nn\phi_t} = \ln \left[\frac{I_0(v_{AP})}{1 + \frac{I_L}{I_S}} \right] \quad v_{AP} = \frac{V_A}{n\phi_t}$$

$$R_O = \frac{V_O - V_L}{I_L} = \frac{Nn\phi_t}{I_S} \frac{\ln \left[1 + \frac{I_L}{I_S} \right]}{\frac{I_L}{I_S}}$$

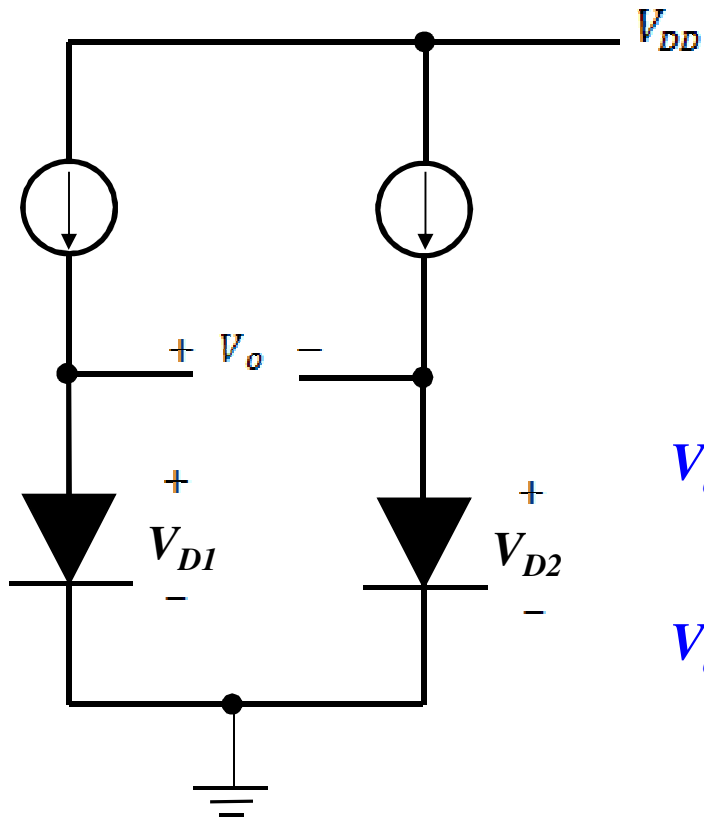


$$R_{in} = \frac{V_A^2}{2P_{in}} \quad R_{in} = \frac{V_A}{2\alpha_P N (I_L + I_S)} \frac{I_0(v_{AP})}{I_1(v_{AP})}$$

$$I_1(v_{ap}) = I'_0(v_{ap})$$

$$C_{RET} \approx N \bar{C}_D$$

Temperature sensor



$$V_o = V_{D1} - V_{D2} = n\phi_t \left[\ln \left(1 + \frac{I_1}{I_S} \right) - \ln \left(1 + \frac{I_2}{I_S} \right) \right]$$

$$V_o \cong n\phi_t \left[\ln \frac{I_1}{I_S} - \ln \frac{I_2}{I_S} \right] = n\phi_t \ln \frac{I_1}{I_2}$$

References

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